# Who Said we Need to Relax All Variables?

Michael Katz, et al. 2013

## Red-Black Planning

- Only relax some variables (colored red)
  - Accumulate values monotonically (delete-relaxed)
- Keep other variables unrelaxed (colored black)
  - Their values change back and forth
- Balancing computational complexity and heuristic accuracy

## Achieving computational efficiency

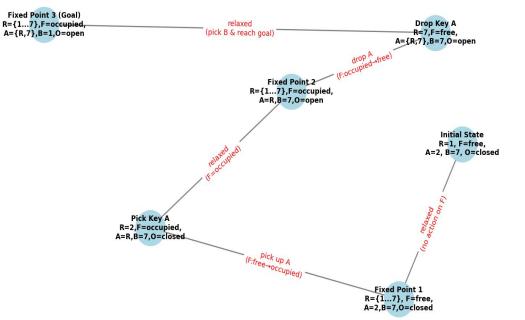
- Number of black variables
  - Limit the number of black variables to a fixed number
- Domain size of black variables
  - Limit the size of the domain for each black variable
- Fewer realistic constraints that must be maintained explicitly

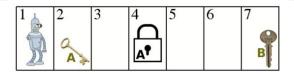
## **Polynomial-Time Result**

### Theorem 1:

Planning for RB tasks with a fixed number of black variables, each having a fixed-size domain, is solvable in polynomial time.

## Single Black Variable Case





#### Hand status F is the only black variable

**Algorithm :** RB2-PLANGEN( $\Pi$ ) main  $/\!/ \Pi = \langle \{v_0\}, V^{\mathsf{R}}, A, I, G \rangle$  $R \leftarrow I$  $R \leftarrow R \cup \text{RelaxedFixedPoint}(A_{\emptyset} \cup A_{I[v_0]})$ if  $G \subseteq R$ then return "solvable" for  $I[v_0] \neq d \in \mathcal{D}(v_0), a_1 \in A_{I[v_0] \rightarrow d}$  s.t.  $\mathsf{pre}(a_1) \subseteq R$  $R \leftarrow R[a_1]$  $R \leftarrow R \cup R$ ELAXEDFIXEDPOINT $(A_{\emptyset} \cup A_d)$ if  $G \subset R$ then return "solvable" for  $a_2 \in A_{d \to I[v_0]}$  s.t.  $\operatorname{pre}(a_2) \subseteq R$ (everywhere in  $\Pi$  and R, do do  $\left\{ \begin{array}{l} \text{replace } I[v_0] \text{ and } d \text{ with a new value } d_{\{I[v_0],d\}} \\ R \leftarrow R \cup \text{RELAXEDFIXEDPOINT}(A) \end{array} \right.$ if  $G \subset R$ then return "solvable" return "unsolvable"

## Limitations of Polynomial-Time Result

- **Theorem 2**: Plan existence for RB tasks with a fixed number of black variables is NP-complete
  - Fixed number of black variables, unbounded domains -> NP-complete

- **Theorem 3**: Plan existence for RB tasks where all black variables have fixed-size domains is PSPACE-complete
  - Unbounded number of black variables, fixed-size domains -> PSPACE-complete

## **Practical Heuristic Computation**

- Full delete-relaxation heuristics **underestimate** true planning costs
- Red-Black heuristics substantially improve heuristic accuracy
  - Directly computing the optimal RB heuristic is NP-hard
  - Focus only on tractable fragments

## **Perfect Red-Black Heuristics**

- Identifying useful, tractable fragments
  - **rSCC** (Reversible Strongly Connected Components)
    - Solvable in polynomial-time
- A Simple Condition for Perfect Red-Black Heuristics
  - **Lemma 4**: If the chosen red variables have no influence on other variables, the RB heuristic will produce perfect estimates.

## How the perfect heuristic condition applies to IPC Benchmarks

- LOGISTICS, MICONIC: Relaxing variables representing object/passenger locations
- SATELLITE: Relaxing variables for capturing image-taking tasks, while leaving satellite status variables black
- VISIT-ALL: Choose visited variables to be red

## Conclusion

- Benefit of Red-Black heuristics
- Identifying which variables to relax Lemma 4
- Exploiting selective relaxations is a promising direction