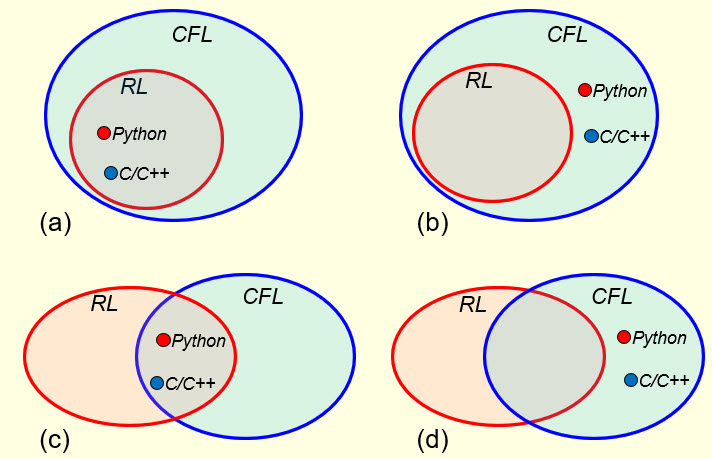
CS375 Homework Assignment 5 (40 points)

Due date: 03/04/2025

1. (2 points)

In the following (a), (b), (c) and (d) four cases, which one is the correct representation of the relationship between Regular Languages (RL) and Context-Free Languages (CFL) and the memberships of the Python and C/C++ programming languages?



Put your answer in the following blank.

1. (5 points)

For the PDA’s shown in Fig. 1 and Fig. 2, which one/ones or no one would accept the language by empty stack? Use the execution of the string*abbba* to justify your answer. The execution should be carried out using ‘Instantaneous Descriptions’.

A diagram of a mathematical equation

AI-generated content may be incorrect.

Fig. 1

A diagram of a function

AI-generated content may be incorrect.

Fig. 2

**Sol.**

For the PDA in Figure 1, we have For the PDA in Figure 2, we have

(0, abbba, X)

(0, abbba, X)

1. (4 points)

The language accepted by the final-state PDA shown in Fig. 1 below is:

(1point)

A diagram of a function

AI-generated content may be incorrect.

The language accepted by the final-state PDA shown in Fig. 2 is:

(1 point)

If the language accepted by the following final-state PDA is:

{

A diagram of a complex function

AI-generated content may be incorrect.

then what is the language accepted by the following final-state PDA?

A diagram of a mathematical equation

AI-generated content may be incorrect.

Put your answer in the following text box. (2 points)

1. (4 points)

The language generated by the following C-F grammar

is . To transform the above C-F grammar to a one-state empty-stack PDA so that the accepted language of the PDA is the same as the language generated by this C-F grammar, we need to construct a set of specific instructions for this PDA. Four instructions have already been constructed below. Construct the remaining instructions for this PDA in the following blanks. You might not need all the provided blanks.

A screenshot of a music sheet

Description automatically generated

1. (10 points)

Given the following empty-stack PDA,

A diagram of a fan with arrows

AI-generated content may be incorrect.

check if the strings *ba*, *ab,* *Ʌ and c* would be accepted by this PDA. Show your work (using instantaneous descriptions) in the following four tables, respectively.

Note that the key here is, whenever the top symbol of the stack is a nonterminal, if the next input symbol to be processed is not a *Ʌ* then you put a *Ʌ* in front of the un-consumed portion of the input string so you can apply one of the seven instructions of the form “” to replace the top symbol of the stack with a sequence of terminals and/or nonterminals.

|  |  |  |  |
| --- | --- | --- | --- |
| *(0, ba, X)* | *(0, ab, X)* | *(0, Ʌ, X)* | *(0, c, X)* |
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1. (8 points)

Given the following empty-stack PDA, (1.2 points for each of the first five blanks)

A diagram of a function

Description automatically generated

the language *L* accepted by the empty-stack PDA is . Note that Ʌ is an element of *L.*

To transform the PDA to a C-F grammar, for each type of the PDA instructions, we need to construct the corresponding grammar productions.

In the following, I list the PDA instructions on the left and you put the corresponding grammar productions in the blanks on the right. We start with Type 4. (5 points)

Type 4:

The start state and the PDA instruction Ʌ,X/pop as shown below gives:

Diagram

Description automatically generated

The start state and the PDA instruction b,X/pop as shown below gives the same production:

A diagram of a bitcoin

Description automatically generated

Type 1:

The PDA instruction Ʌ,X/pop by itself as shown below gives:

Shape

Description automatically generated

The PDA instruction b,X/pop by itself as shown below gives:

A red line with a line in the middle

Description automatically generated with medium confidence

Type 3:

The PDA instruction a,X/push(X) together with Ʌ,X/pop and b,X/pop as shown below gives:

A diagram of a mathematical equation

Description automatically generated

There are no productions in the Type 2 category because there are no PDA instructions that perform nop stack operation.

Collecting all the productions, we get a context-free grammar whose production set is as follows:

A picture containing table

Description automatically generated (0 points)

After simplification, we get

Shape

Description automatically generated with low confidence (2 points)

or

S

(2 points)

(you only have to answer one case) and it is easy to see that this is a C-F grammar for *L*.

1. (7 points)

Given the following empty-stack PDA, (4 points for the first 8 blanks)

Diagram

Description automatically generated

the language *L* accepted by the empty-stack PDA is the set of strings over the alphabet

{a, b} such that each string has the same number of a’s and b’s.

To transform the PDA into a C-F grammar, for each type of the PDA instructions, we need to construct the corresponding grammar productions.

In the following, put the corresponding grammar productions in the blanks on the right for the instructions shown on the left.

Type 4:

The start state and the PDA instruction Ʌ,X/pop as shown below gives:

Diagram

Description automatically generated

Type 1:

The PDA instruction Ʌ,X/pop by itself as shown below gives:

Shape

Description automatically generated with medium confidence

The PDA instruction a,b/pop by itself as shown below gives:

A picture containing shape

Description automatically generated

The PDA instruction b,a/pop by itself as shown below gives:

Shape, rectangle

Description automatically generated

Type 3:

The PDA instruction a,X/push(a) together with the instructions b,a/pop and Ʌ,X/pop as shown below gives:

A picture containing text, device, meter

Description automatically generated

The PDA instruction b,X/push(b) together with the instructions a,b/pop and Ʌ,X/pop as shown below gives:

A picture containing text, device, meter, gauge

Description automatically generated

The PDA instruction a,a/push(a) together with the instruction b,a/pop (used twice) as shown below gives:

A picture containing text, device, meter, gauge

Description automatically generated

The PDA instruction b,b/push(b) together with the instruction a,b/pop (used twice) as

shown below gives:

A picture containing text, device

Description automatically generated

There are no Type 2 productions because there are no PDA instructions that perform nop stack operation.

Collecting all the productions, we get a context-free grammar whose production set is as follows:

Table

Description automatically generated with medium confidence (0 points)

After simplification, we get

A picture containing text, shoji

Description automatically generated (1 point for S; 1 point for A; 1 point for B)

and it is easy to see that this is a C-F grammar for *L*.

* Solutions must be typed (word processed) and submitted both as a pdf file and a word doc file to Canvas before 23:59 on 03/04/2025.
* Don’t forget to name your files as

CS375\_2025s\_HW5\_LastName.docx / CS375\_2025s\_HW5\_LastName.pdf